



**BENHA UNIVERSITY**  
**FACULTY OF ENGINEERING (SHOUBRA)**  
**ELECTRONICS AND COMMUNICATIONS ENGINEERING**



CCE 304

Measurements and Instrumentations  
(2022 - 2023) term 231

Lecture 4: Electromechanical Instruments (part3).

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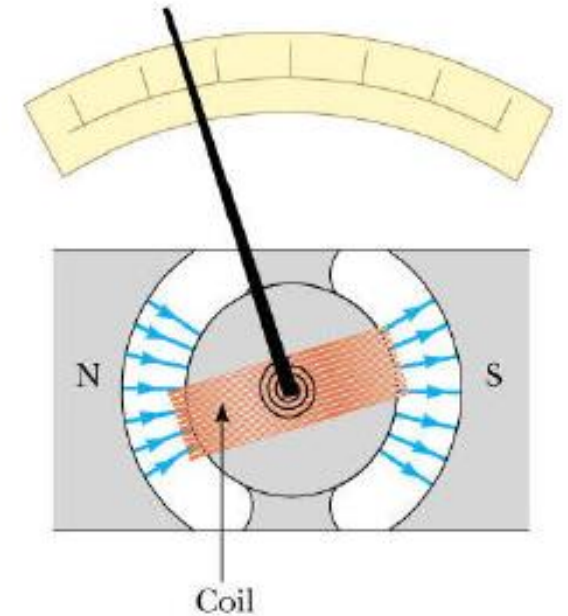
# Chapter Outline:

- 1) Permanent Magnet Moving Coil (PMMC).
- 2) Galvanometer.
- 3) DC Ammeters
- 4) DC Voltmeters
- 5) Ohmmeters
- 6) **AC Voltmeters**
- 7) AC Ammeters

## 3.6 AC Voltmeter: Introduction:

### PMMC as AC instrument:

- ▶ When an alternating current with a **very low frequency 0.1 Hz** is passed through a PMMC, the **pointer will follow the instantaneous level** of the ac signal.
- ▶ Since the PMMC is polarized, **the pointer will move when ac goes positive only** and will stop when ac goes negative.
- ▶ With higher frequencies, the PMMC will **not be able to follow** the changing ac level and the pointer will stop on the **average level** (zero for pure sinusoidal wave).
- ▶ So, a modification has to be done on PMMC to measure alternating current and voltage.

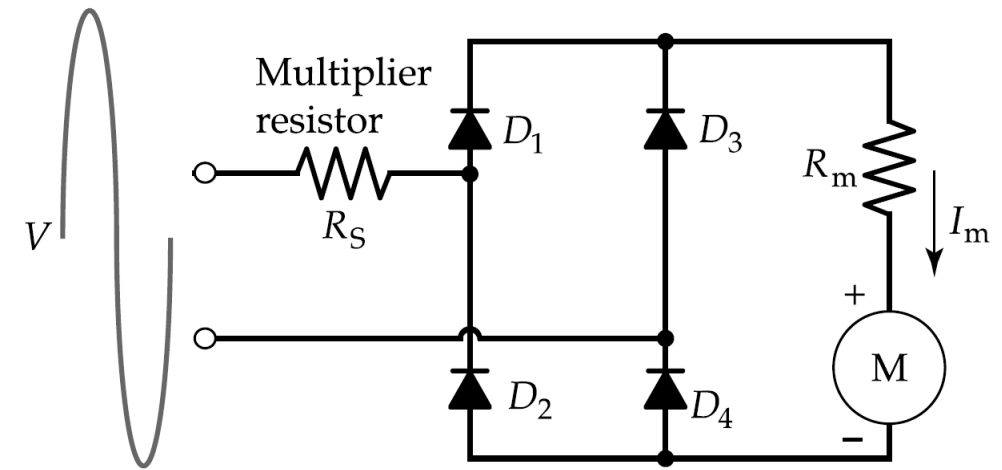


Construction of PMMC

## 3.6 AC Voltmeter:

### [1] Full-Wave Rectifier Voltmeter:

- ▶ **Four diodes rectifiers** are added to the PMMC to convert the AC signal into a series of **uni-directional current pulses** that pass through the PMMC instrument to **cause positive deflection**.
- ▶ **On positive half cycle:** Diodes **D1** and **D4** **conduct** and the current flows through the PMMC meter from **top to bottom**.
- ▶ **On negative half cycle:** Diodes **D2** and **D3** to **conduct** causing the current to flow again through the meter in the same direction.
- ▶ The **multiplier resistance  $R_s$**  is connected to allow **higher voltage** to the meter in the same way as in the case of DC voltmeter.

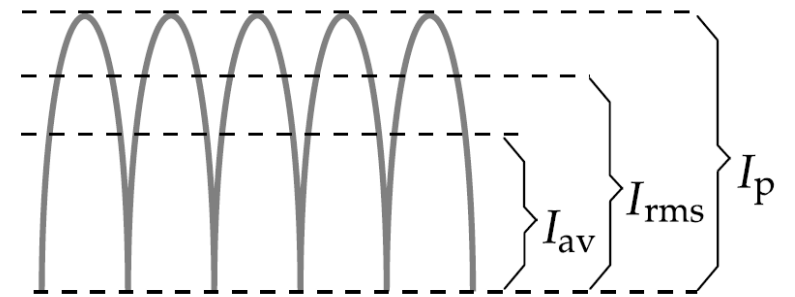


**Figure 4-7** An ac voltmeter may be constructed of a PMMC instrument, a multiplier resistor, and a full-wave bridge rectifier.

## 3.6 AC Voltmeter:

### [1] Full-Wave Rectifier Voltmeter:

- ▶ The rectifier meter will deflect in proportional to the average value of the current (0.637 peak current).
- ▶ However, the meter must indicate the RMS value, (that is, 0.707 peak value) of the voltage.
- ▶ Therefore, the linear scale of the meter can be calibrated accordingly to indicate the RMS value (1.11 average value).
- ▶ Limitation: The diodes drop will limit the measurement of low levels of AC signals.



## Example 3.9

A PMMC instrument with FSD = 100  $\mu\text{A}$  and  $R_m = 1 \text{ k}\Omega$  is to be employed as an ac voltmeter with FSD = 100 V (rms). Silicon diodes are used in the bridge rectifier circuit of Figure 3-17. Calculate the multiplier resistance value required.

### Solution

At FSD, the average current flowing through the PMMC instrument is

$$I_{av} = 100 \mu\text{A}$$

$$\text{peak current } I_m = \frac{I_{av}}{0.637} = \frac{100 \mu\text{A}}{0.637} \approx 157 \mu\text{A}$$

$$I_m = \frac{(\text{applied peak voltage}) - (\text{rectifier volt drop})}{\text{total circuit resistance}}$$

$$\text{rectifier volt drops} = 2V_F \text{ (for } D_1 \text{ and } D_4 \text{ or } D_2 \text{ and } D_3)$$

$$\text{applied peak voltage} = 1.414V_{rms}$$

$$\text{total circuit resistance} = R_s + R_m$$

$$I_m = \frac{1.414V_{rms} - 2V_F}{R_s + R_m}$$

$$R_s = \frac{1.414V_{rms} - 2V_F}{I_m} - R_m$$

$$= \frac{(1.414 \times 100 \text{ V}) - (2 \times 0.7 \text{ V})}{157 \mu\text{A}} - 1 \text{ k}\Omega$$

$$= 890.7 \text{ k}\Omega$$

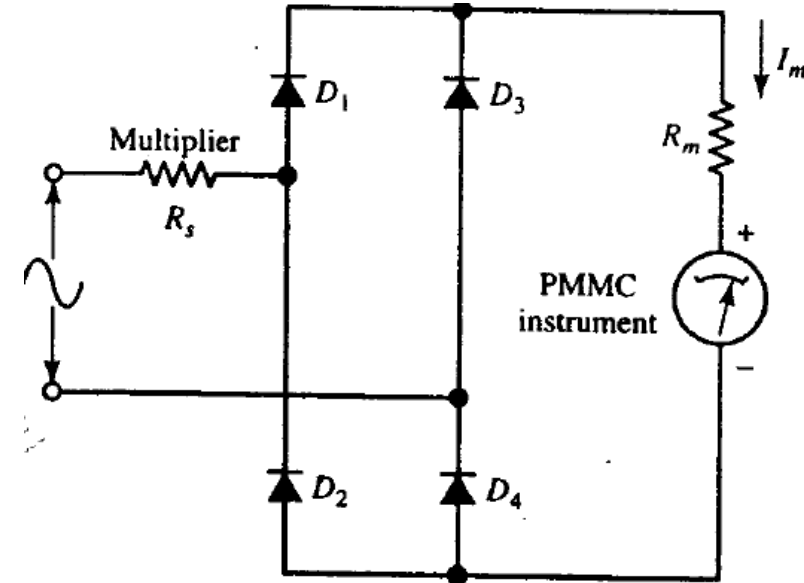


Fig. 3-17

## Example 3.10:

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- Calculate the pointer indications for the voltmeter in the previous example, when the rms input voltage is: (a) 75 V and (b) 50 V

### **Solution**

$$\begin{aligned} \text{(a)} \quad I_{av} &= 0.637 I_m = 0.637 \left( \frac{1.414 V_{rms} - 2V_F}{R_s + R_m} \right) \\ &= 0.637 \left[ \frac{(1.414 \times 75 \text{ V}) - (2 \times 0.7 \text{ V})}{890.7 \text{ k}\Omega + 1 \text{ k}\Omega} \right] \\ &\approx 75 \mu\text{A} = 0.75 \text{ FSD} \end{aligned}$$

$$\begin{aligned} \text{(b)} \quad I_{av} &= 0.637 \left[ \frac{(1.414 \times 50 \text{ V}) - (2 \times 0.7 \text{ V})}{890.7 \text{ k}\Omega + 1 \text{ k}\Omega} \right] \\ &\approx 50 \mu\text{A} = 0.5 \text{ FSD} \end{aligned}$$

The previous two examples demonstrate that:

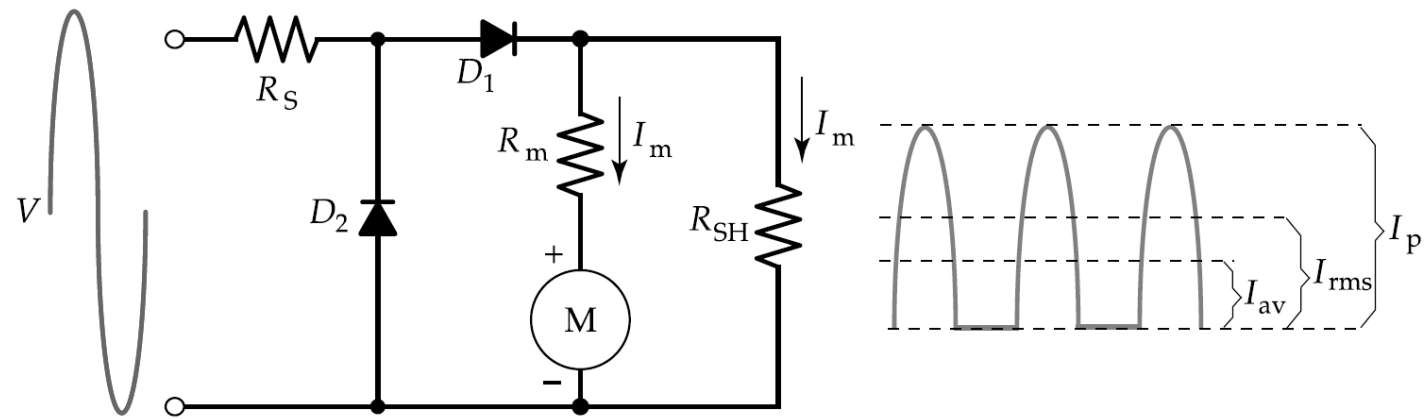
100V rms at Full scale, 75V rms at 0.75 FSD and 50V rms at 0.5 FSD.

Then, the instrument has a linear scale

## 3.6 AC Voltmeter:

### [2] Half-Wave Rectifier Voltmeter:

- ▶ **D1** is used to rectify the ac signal into the PMMC.
  - ▶ **On positive half cycle:** Diodes **D1** conducts and the current flows through the PMMC.
  - ▶ **On negative half cycle:** Diodes **D1** is OFF and no current flows.
- **R<sub>SH</sub>** is added in **parallel** to increase the current in diode **D1** when a positive half-wave appears at the input (to operate in the linear region of the diode).
  - **D2** is added to **protect** the meter against any reverse voltages.
  - The rectifier meter will deflect in proportional to the average value of the current ( $0.5 * 0.637 * \text{peak current}$ ).



**Figure 4-8** Half-wave rectification may be used with a PMMC instrument and a multiplier resistor for ac voltage measurements. A shunt resistor ( $R_{SH}$ ) is included to ensure a satisfactory rectifier forward current level. The additional rectifier ( $D_2$ ) minimizes reverse leakage current through  $D_1$ .



## Example 3.11:

A PMMC instrument with  $FSD = 50 \mu\text{A}$  and  $R_m = 1700 \Omega$  is used in the half-wave rectifier voltmeter circuit illustrated in Figure 3-18. The silicon diode ( $D_1$ ) must have a minimum (peak) forward current of  $100 \mu\text{A}$  when the measured voltage is 20% of FSD. The voltmeter is to indicate  $50 \text{ V rms}$  at full scale. Calculate the values of  $R_s$  and  $R_{SH}$ .

**Solution** At FSD,  $I_{av} = 50 \mu\text{A}$

Meter peak current:  $I_m = \pi I_{av} = \pi(50 \mu\text{A}) = 157 \mu\text{A}$

At 20% of FSD, diode peak current  $I_F$  must be at least  $100 \mu\text{A}$ ; therefore, at 100% of FSD,

$$I_{F(\text{peak})} = \frac{100\%}{20\%} \times 100 \mu\text{A} = 500 \mu\text{A}$$

$$I_{F(\text{peak})} = I_m + I_{SH}$$

$$\begin{aligned} I_{SH(\text{peak})} &= I_{F(\text{peak})} - I_m \\ &= 500 \mu\text{A} - 157 \mu\text{A} = 343 \mu\text{A} \end{aligned}$$

$$\begin{aligned} V_{m(\text{peak})} &= I_m R_m = 157 \mu\text{A} \times 1700 \Omega \\ &= 266.9 \text{ mV} \end{aligned}$$

$$R_{SH} = \frac{V_{m(\text{peak})}}{I_{SH(\text{peak})}} = \frac{266.9 \text{ mV}}{343 \mu\text{A}} = 778 \Omega$$

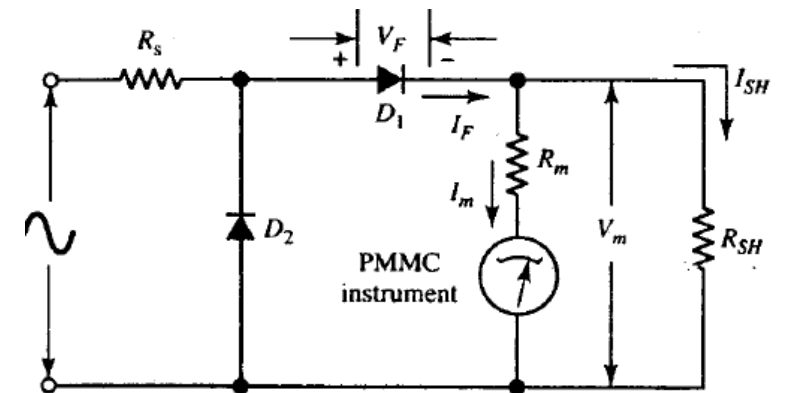


Fig. 3-18

# Solution (Cont.)

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$$I_{F(\text{peak})} = \frac{(\text{applied peak voltage}) - V_{m(\text{peak})} - V_F}{R_s}$$

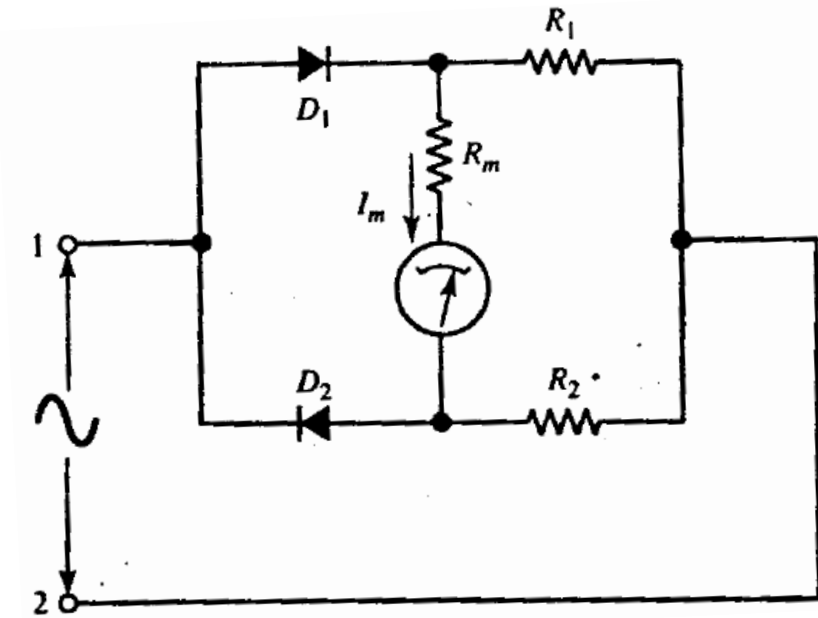
$$I_{F(\text{peak})} = \frac{1.414V_{\text{rms}} - V_{m(\text{peak})} - V_F}{R_s}$$

$$\begin{aligned} R_s &= \frac{1.414V_{\text{rms}} - V_{m(\text{peak})} - V_F}{I_{F(\text{peak})}} \\ &= \frac{(1.414 \times 50 \text{ V}) - 266.9 \text{ mV} - 0.7 \text{ V}}{500 \mu\text{A}} \\ &= 139.5 \text{ k}\Omega \end{aligned}$$

## 3.6 AC Voltmeter:

### [3] Half-bridge full-wave rectifier Voltmeter

- ▶ **Two diodes and two resistors** are used instead of the **four diodes** used in a full-wave bridge rectifier.
  - ▶ During **the positive half-cycle**, **D1 is forward** and D2 is reverse. Current flows from **terminal 1** through **D1** and the **meter**, and then through **R2** to **terminal 2**
  - ▶ R1 is in parallel with the meter and R2.
- 
- During **the negative half-cycle**, **D2 is forward** biased and D1 is reverse biased. Current now flows from **terminal 2** through **R1** and the **meter**, and through **D2** to **terminal 1**.
  - R2 is in parallel with the series-connected meter and R1.

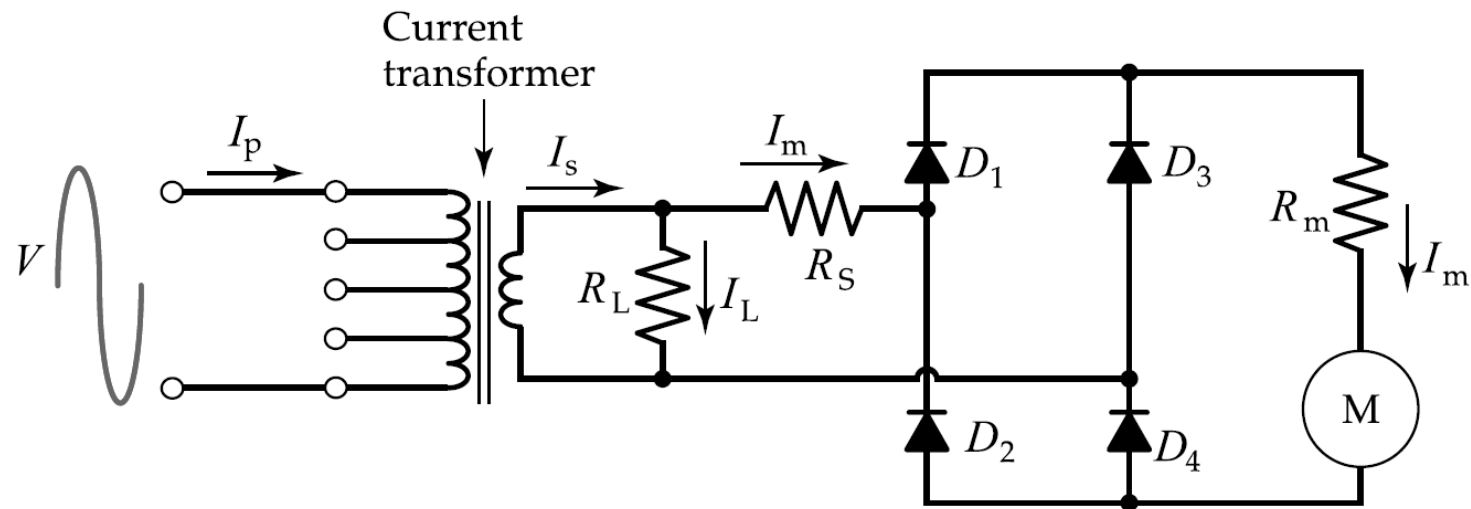


# Chapter Outline:

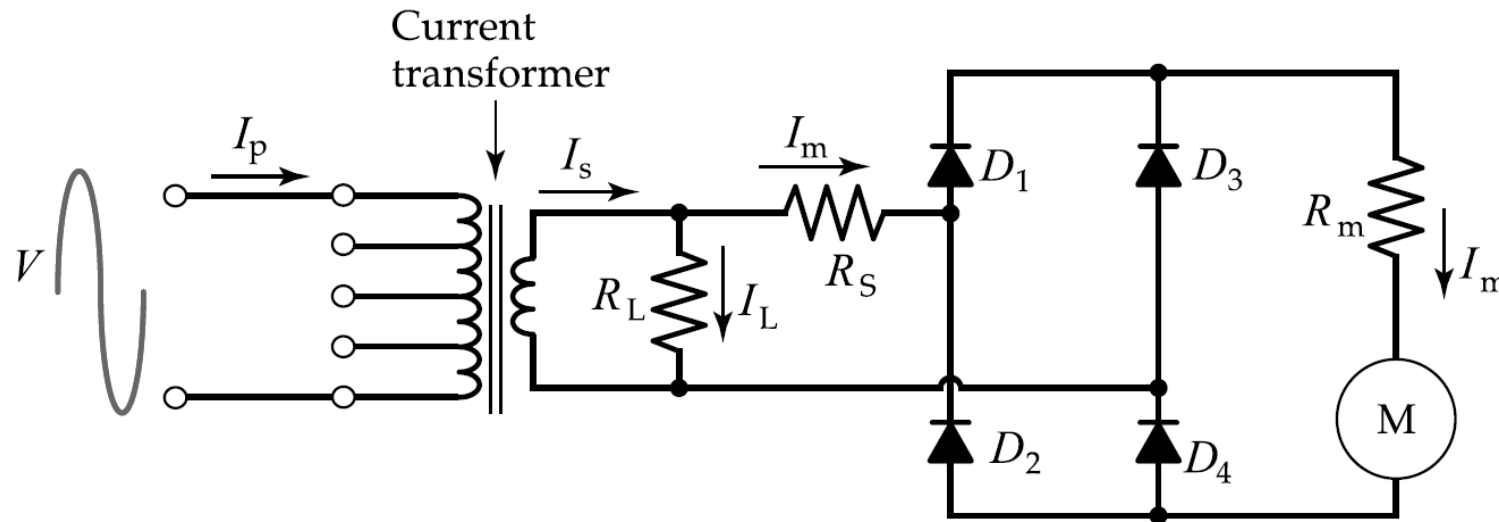
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## 3.7 AC Ammeter:

- ▶ The requirement of the AC ammeter is to have very **low resistance** which implies that **a very low** (typically less than 100 mV) **voltage drop**.
- ▶ Thus, a rectifier PMMC circuit is not suitable to directly measure AC currents.
- ▶ **A step-up transformer** is used to measure AC current:



**Figure 4-10** Ac ammeter circuit consisting of a current transformer, full-wave bridge rectifier, and a PMMC instrument.



- ▶ Using a **current transformer** with a rectifier instrument provides a **very low terminal resistance and low voltage drop**.
- ▶ In step-up transformer, the input voltage gets stepped up so that sufficient voltage can be provided for rectifier operation.
- ▶ Since the transformer is used in an ammeter circuit, the current transformation ratio  $I_p/I_s = N_s/N_p$  is very important.
- ▶ A **multi-range AC ammeter** could be provided by changing the **number of primary turns in the transformer** or using **different values of load resistance ( $R_L$ )**

## Example 3.12:

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A rectifier ammeter with the circuit shown is to give FSD for a primary current of 250 mA (rms). The **PMMC meter has FSD = 1 mA** and  $R_m = 1700 \Omega$ . The current transformer has  $N_s = 500$  and  $N_p = 4$ . The diodes each have  $V_F = 0.7 \text{ V}$ , and the series resistance is  $R_S = 20 \text{ k}\Omega$ . **Calculate** the required value of  $R_L$ .

**Solution:**

$$\begin{aligned} \text{Peak meter current } I_m &= \frac{I_{av}}{0.637} = \frac{1 \text{ mA}}{0.637} \\ &= 1.57 \text{ mA} \end{aligned}$$

*Transformer secondary peak voltage,*

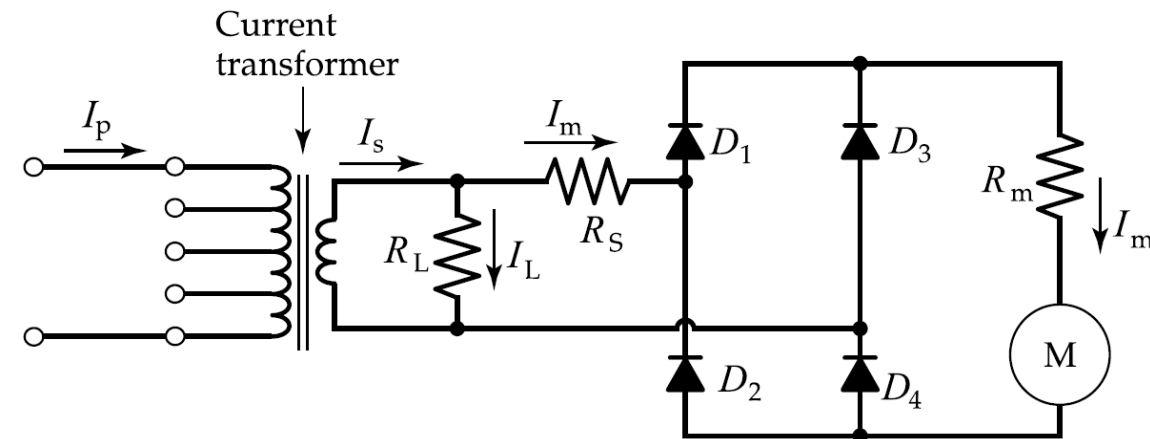
$$\begin{aligned} E_m &\doteq I_m(R_S + R_m) + 2V_F \\ &= 1.57 \text{ mA} (20 \text{ k}\Omega + 1700 \Omega) + 1.4 \text{ V} \\ &\approx 35.5 \text{ V} \end{aligned}$$

*or secondary voltage*

$$\begin{aligned} E_s &= (0.707 \times 35.5 \text{ V}) \text{ rms} \\ &\approx 25.1 \text{ V} \end{aligned}$$

*and*

$$\begin{aligned} \text{rms meter current} &= 1.11 I_{av} \\ &= 1.11 \text{ mA} \end{aligned}$$



## Solution (Cont.)

*Transformer rms secondary current,*

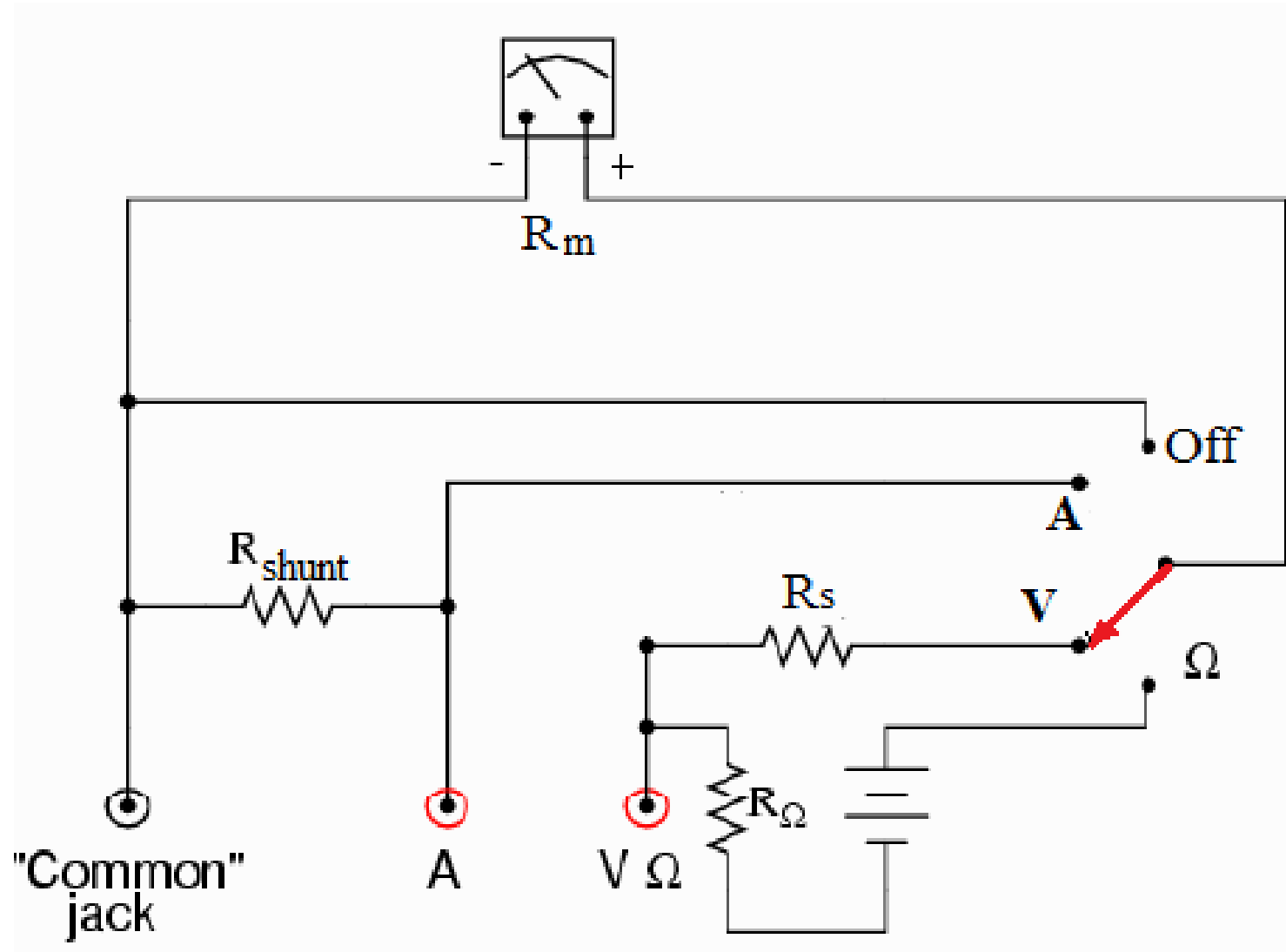
$$\begin{aligned} I_s &= I_p \frac{N_p}{N_s} \\ &= 250 \text{ mA} \times \frac{4}{500} = 2 \text{ mA} \end{aligned}$$

$$\begin{aligned} I_L &= I_s - I_m \\ &= 2 \text{ mA} - 1.11 \text{ mA} = 0.89 \text{ mA} \end{aligned}$$

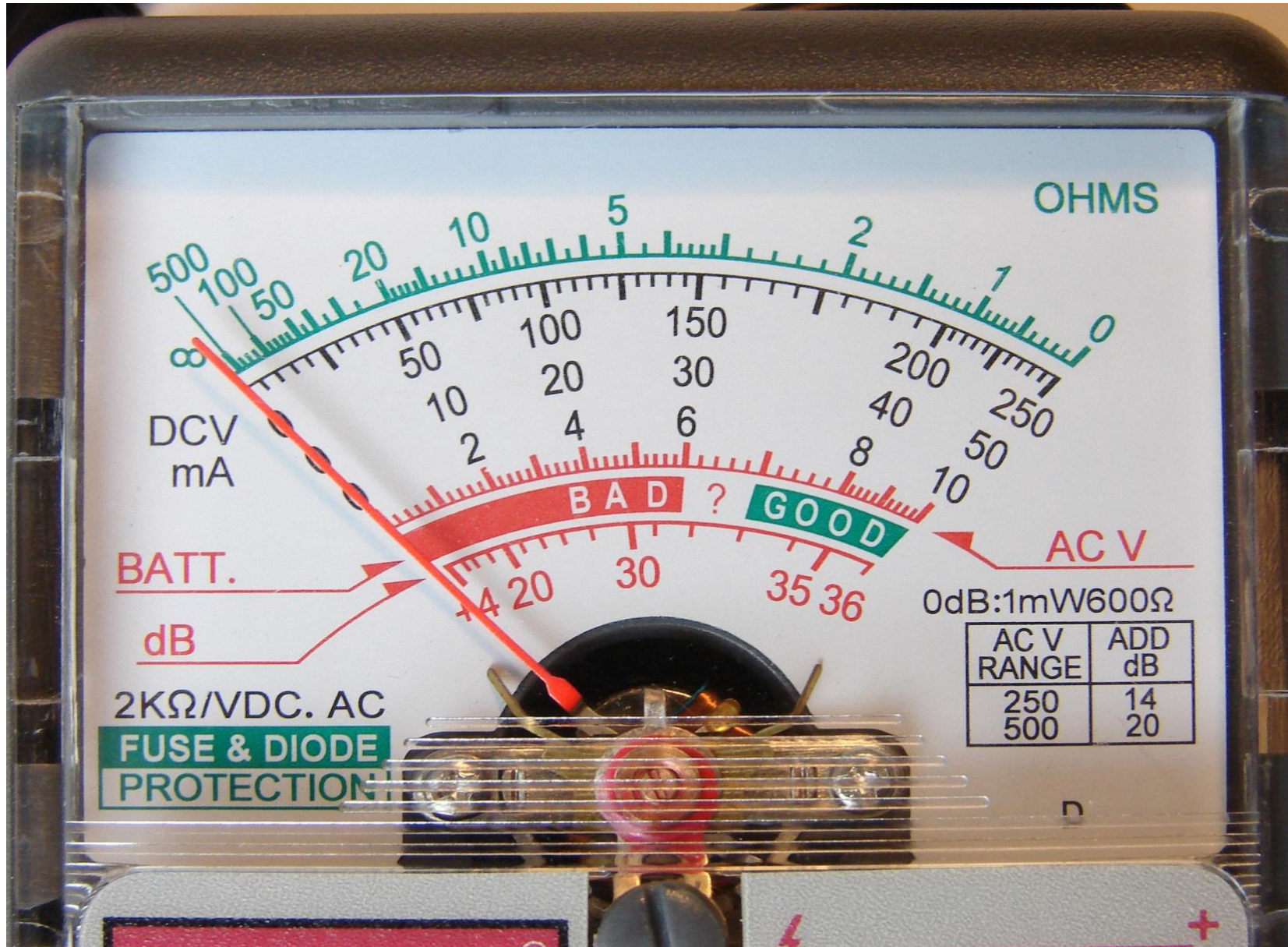
$$\begin{aligned} R_L &= \frac{E_s}{I_L} = \frac{25.1 \text{ V}}{0.89 \text{ mA}} \\ &= 28.2 \text{ k}\Omega \end{aligned}$$



## Analogue Multi-meter circuit



# Scale of ohm, volt and ampere in analogue multi-meter





**END OF LECTURE**

**BEST WISHES**